

Optimal Scheduling in High Speed Downlink Packet Access Networks

by

Hussein Al-Zubaidy, Jerome Talim, Ioannis Lambadaris

SCE-Carleton University

November 27, 2006

Abstract

High-Speed Downlink Packet Access (HSDPA) provides high cell peak data rate (up to 10.8 Mbps) on the downlink by incorporating Adaptive Modulation and Coding (AMC) and fast scheduling. Scheduling is one of the most important QoS control approaches in this system, and can significantly affect overall system performance.

In this report, we present an analytic model and methodology to determine optimal scheduling policy that involves two dimension space allocation: *time* and *code*, in High Speed Downlink Packet Access (HSDPA) system. A discrete stochastic dynamic programming model for the HSDPA downlink scheduler is presented. Value iteration is then used to solve for optimal policy. This framework is used to find the optimal scheduling policy for the case of two users sharing the same cell. Simulation is used to study the performance of the resulted optimal policy using Round Robin (RR) scheduler as a baseline. The results showed that the optimal policy can achieve up to 30% higher throughput compared to RR.

The policy granularity is introduced to reduce the computational complexity by reducing the action space. In this case, chunks of codes will be allocated to users rather than individual codes. The smaller the chunk size, the finer the policy granularity. The results showed that finer granularity (down to 5 codes) enhances the performance significantly. However, the enhancement gained when using even finer granularity was marginal and does not justify the added complexity. The results also showed that in heavy loading conditions, this enhancement will diminish, and a coarser policy might even perform slightly better than a finer one.

The behaviour of the value function was observed to characterize the optimal scheduling policy. These observations are then used to develop a heuristic scheduling policy. The performance of the heuristic policy was studied. The results showed that the devised heuristic policy performs very close to the optimal policy. It has much less computational complexity which makes it easy to deploy and with only slight reduction in performance compared to the optimal policy.

Contents

1	Introduction	3
2	Problem Definition	5
2.1	HSDPA Downlink Scheduler Abstraction	5
2.2	HSDPA Downlink Channel Model	6
3	Model Description	7
3.1	Basic Assumptions	7
3.2	FSMC State Space	8
3.3	State and Action Sets	8
3.4	Reward Function	9
3.5	Transition Probability function	10
3.6	Value Function	11
4	Two Users with 2-State FSMC	11
4.1	Optimal Policy Structure	12
4.1.1	Optimal Policy for Two Symmetrical Users	12
4.1.2	The Effect of Channel Quality on Policy Structure	13
4.1.3	The Effect of Arrival Probability on Policy Structure	13
5	The Heuristic Policy	13
5.1	Heuristic policy ($c = 15$)	17
5.2	Heuristic Policy ($c = 5$)	17
5.3	Heuristic Policy ($c = 3$)	19
5.4	Other Considerations	19
6	Performance Evaluation	22
6.1	The Effect of Policy Granularity	22
6.2	Heuristic Policy Evaluation	25
6.3	Computational Complexity	29
7	Conclusion	30
	APPENDIX A	31
	APPENDIX B	33
	APPENDIX C	35

List of Figures

1	HSDPA scheduler model (downlink).	6
2	FSMC model for HSDPA downlink channel.	6
3	The optimal policy for two user case; $c = 15$	14
4	The optimal policy for two user case; $c = 5$	15
5	The optimal policy for two user case; $c = 3$	16
6	The heuristic policy (dotted line) in comparison to the optimal policy; $c = 15$	18
7	The heuristic policy (dotted line) in comparison to the optimal policy; $c = 5$	20
8	The heuristic policy (dotted line) in comparison to the optimal policy; $c = 3$	21
9	The effect of policy granularity on queue length	23
10	The effect of policy granularity on the average queueing delay experienced by the two users	24
11	The effect of policy granularity on scheduler throughput	24
12	The effect of policy granularity on scheduler dropping probability	25
13	System throughput for different loading conditions.	26
14	Queueing delay performance, $P(\gamma_1 = 1) = 0.84$, $P(\gamma_2 = 1) = 0.5$, $q_1 = 0.8$, $q_2 = 0.5$ and $u = 10$	26
15	Queue length, $\rho = 0.75$, $P(\gamma_1 = 1) = 0.84$, $P(\gamma_2 = 1) = 0.5$, $q_1 = 0.5$, $q_2 = 0.5$ and $u = 10$	27
16	Queue length, $\rho = 1.0$, $P(\gamma_1 = 1) = 0.84$, $P(\gamma_2 = 1) = 0.5$, $q_1 = 0.8$, $q_2 = 0.5$ and $u = 10$	28
17	Queue length, $\rho = 1.1$, $P(\gamma_1 = 1) = 0.6$, $P(\gamma_2 = 1) = 0.6$, $q_1 = 0.8$, $q_2 = 0.5$ and $u = 10$	28
18	Two queue model with shared server and random channel connectivity	35

1 Introduction

The rapid development of wireless technology enables the implementation of services which are so far available only on IP based networks. Each service has its own requirements, in terms of bandwidth (Web browsing service for instance), or Quality of Service (QoS) for real-time applications such as Voice over IP. The increasing demand on such services triggered the evolution of third generation wireless networks toward an IP based Packet-switched networks. The new 3G systems (e.g., HSDPA) were designed to have an IP-based infrastructure that enables the reuse of the available IP resources and technologies and in order to reduce the cost [1]. Nevertheless, the added packet switching capability introduced new challenges that have to be dealt with.

One of the challenges is to meet the QoS requirements of the offered services. Wireless links in general have different channel characteristics than that of wireline links. They are subject to time- and location-dependent signal attenuation, fading and interference, which will result in bursty errors and time varying channel capacities. Therefore, the direct application of the available wireline QoS techniques is impractical. Furthermore, it is extremely difficult to provide hard (absolute) QoS guarantees and only soft QoS (Differentiated services) can be provided [2]. Packet scheduling is one of the most important QoS control approaches for wireless communications [3]. The scheduling algorithms in wireless systems should take into consideration the variation in channel characteristics, make use of the user diversity to maximize throughput, and aim at providing all users with a fair access to the network.

Scheduling in HSDPA systems involves not only *Transmission Time Intervals (TTI) allocation* but also *codes allocation*. On the downlink, HSDPA uses Code and Time Division Multiplexing (CDM/TDM) and has 15 codes to be allocated per TTI. Most of the available work in scheduler design (e.g. [2], [5] and [6]) is based on intuition and creativity of the designers. The designer usually selects an optimization criterion that represents some important performance measure (in his/her opinion) and builds an algorithm based on that criteria, and then tries to establish confidence in it using backward analysis or simulation. This approach can be described as a *procedural approach*. This, most likely, will result in a suboptimal algorithm at the best, that performs well in some scenarios and poor in the others. This happens especially in systems such as HSDPA, since it uses a very complex set of features such as Hybrid Automatic Repeat reQuest (H-ARQ) and Adaptive Modulation and

Coding (AMC). These features introduced many new and interrelated tuning parameters which cannot be grasped by one selected criterion. Another observation is the lack of work on schedulers that dynamically allocate codes as well as TTI for the users in the system.

This work presents a novel approach for scheduling. An analytic model, using stochastic dynamic programming is built to represent the HSDPA scheduler with some realistic assumptions to the rest of the system components. This model is a simplifying abstraction of the real scheduler which estimates system behaviour under different conditions and describes the role of various system components in these behaviours. This model can be solved numerically to obtain the optimal code allocation policy for some given *objective function* in a straight forward manner.

This approach can be considered as a *unified approach* since the same model can be used when solving for different objective function by simply changing the reward associated with the model to reflect the new objective. Different objective functions may result in different optimal policies. For example, if the objective is to maximize the cell throughput, then greedy C/I scheduler can achieve this goal by favouring the user with the best channel conditions. However, using this policy will starve the users with poor channel quality. On the other side of spectrum, Round Robin (RR) scheduler will divide the resources fairly between all the users in the cell to achieve fairness on the expense of cell throughput. The optimal policy lies somewhere in the middle and depends on what degree of fairness is required. The proposed approach produces an optimal policy in the sense that it maximize cell throughput for a given fairness criteria. It provides an elegant and presentable analytic foundation for scheduling problems and may be used as a benchmarking tool to the other schedulers.

2 Problem Definition

Third generation release R'5 [1][4], also called High-Speed Downlink Packet Access (HSDPA), is an IP-based network that can offer users a high speed asymmetric radio link with downlink peak bit rate up to 10.8 Mbps. The HSDPA uses a single time shared channel (HS-DSCH) per cell/sector. This channel is divided into 2 ms Transmission Time Intervals (TTI). Each TTI may be used to transfer packets to one or more users at a rate that depends on their User Equipment (UE) capabilities and needs. The UE can use up to 15 codes simultaneously to achieve higher rate. More than one user can share the same slot by dividing the available 15 codes between them. In such case, the scheduler need not only to choose the next user/users to be served, but also the number of codes each user will receive.

The problem can be stated as follows: devise a methodology to find the optimal scheduling regime that controls the allocation of the time-code resources fairly between all the active users while maximizing the overall cell throughput. The scheduling algorithm should provide channel aware, high speed and fair resource allocation.

2.1 HSDPA Downlink Scheduler Abstraction

The HSDPA downlink channel uses a mix of Time Division Multiplexing and Code Division Multiplexing:

- Time is slotted into fixed length 2 ms TTIs.
- During each TTI, there are 15 available codes that may be allocated to one or more users.

During one TTI, the channel capacity associated to one single user depends on the number of allocated codes and on the channel condition. This is mainly due to the fact that HSDPA uses AMC to adapt the transmission rate to the current channel conditions. A mobile user with good channel conditions will experience higher data rate than the other users.

The diagram in Figure 1 depicts a conceptual realization of the HSDPA downlink scheduler. Different users have separate buffers in the base station (Node-B according to 3GPP), and they are competing for the system resources. Channel state monitor/predictor is necessary to monitor current channel conditions of each user and predict his channel state during the next

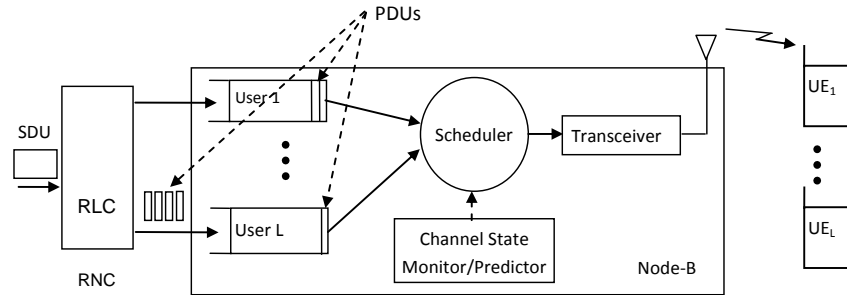


Figure 1: HSDPA scheduler model (downlink).

TTI. This information will then be used to adapt the transmission rate to the expected channel conditions. The arrived Service Data Units (SDU) are assumed to be segmented by the Radio Link Control (RLC) into u_i fixed size Protocol Data Units (PDU) before delivering them to Node-B. The PDUs then will be classified and inserted into the proper buffers awaiting transmission to the intended user. RNC is the Radio Network Controller unit which implements the RLC protocol.

2.2 HSDPA Downlink Channel Model

The wireless channel for the HSDPA system is modelled as a Finite-State Markov Channel (FSMC) following [8]. This is done by partitioning the signal to noise ratio (SNR) into finite number of intervals, each representing a state in a Markov Chain. Assuming that the fading is slow enough that the channel states for consecutive time epochs are neighbouring states, then the model will be reduced into a discrete time birth and death process, as shown in Figure 2.

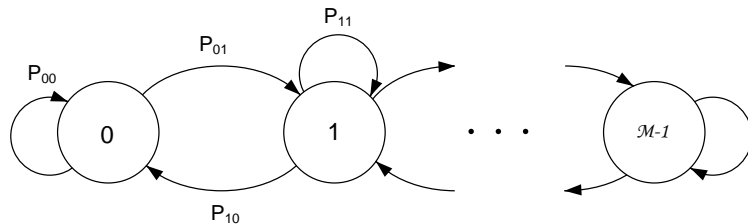


Figure 2: FSMC model for HSDPA downlink channel.

Depending on the expected SNR state, different modulation and error-correcting coding rates can be dynamically selected from a set of Modulation and Coding Schemes (MCS) [7]. The higher the order of the MCS selected the higher the transmission rate. The SNR is mapped directly into MCS and hence into data rates. In light of this, the states in our channel model will equivalently represent data rate levels rather than SNR.

3 Model Description

In this section, we propose an approach, based on Markov Decision Process (MDP), to find the optimal code allocation policy for the HSDPA downlink scheduler. We present a general model for this system and suggest a reward function that achieve the objective function.

To describe a system as a MDP model, the states, actions, rewards and transition probabilities have to be defined first. In our proposed model, time is slotted in constant intervals of size Δt . Let T denote the set of decision epochs of the system, and $T = \{1, 2, \dots\}$. At time $t \in T$, we define $\mathbf{s}(t)$ and $\mathbf{a}(\mathbf{s})$ as the system state and the action taken at that state. HSDPA downlink scheduler is modelled by the 5-tuple $(T, S, A, P_{ss'}(\mathbf{a}), R(\mathbf{s}, \mathbf{a}))$, where S and A are the state and action spaces, $P_{ss'}(\mathbf{a}) = Pr(\mathbf{s}(t+1) = \mathbf{s}' | \mathbf{s}(t) = \mathbf{s}, \mathbf{a}(\mathbf{s}) = \mathbf{a})$ is the state transition probability, and $R(\mathbf{s}, \mathbf{a})$ is the immediate reward when at state \mathbf{s} and taking action \mathbf{a} .

3.1 Basic Assumptions

There are L active users in the cell. A user $i \in I = \{1, 2, \dots, L\}$ is allocated a buffer of size B_i . For the sake of simplicity, we will assume that $B_i = B$ for all $i \in I$. Error free transmission is assumed for eliminating the need for retransmission queue. SDUs arrive at the RNC during the current TTI will be segmented by RLC into a fixed number of PDUs (u_i) and delivered to Node-B to be inserted into their respected buffer at the beginning of the next TTI.

For each user $i \in I$ and slot $t \in T$, we define:

- $y_i(t)$ the number of scheduled PDUs,
- $x_i(t) \in \mathcal{X} = \{0, 1, 2, \dots, B\}$ the queue size,

- $z_i(t) \in \{0, u_i\}$ the number of arriving PDUs.

The SDUs destined to user i arrives at the RNC during one TTI according to the Bernoulli distribution with parameter q_i . Arrivals are assumed to be independent of the system state and of each other. PDU size is chosen to be equal to the minimum Transport Format and Resource Combination (TFRC) for one code (i.e., one code is needed to transmit one PDU when the channel is in state 1). The scheduler can assign the available 15 codes as chunks of c codes at a time to active users in the system. The chunk size c must divide the total number of codes (15); therefore, $c \in \{1, 3, 5, 15\}$. For example, choosing $c = 5$ means that the policy can assign 0, 5, 10, or 15 of the available 15 codes to any user at any given TTI.

3.2 FSMC State Space

The channel state of user i during slot t is denoted by $\gamma_i(t)$; and its associated channel state space is the set $\mathcal{M} = \{0, 1, \dots, M - 1\}$, where M is the total number of available channel states. \mathcal{M} constitutes a subset of the available MCS set recommended by 3GPP. The elements of \mathcal{M} were ordered in a way such that $\gamma_i(t)$ is directly proportional to the number of PDUs that can be transmitted by user i in one TTI. This ordering is necessary to reduce computational complexity. Furthermore, we assume that user i channel can handle up to $\gamma_i(t)$ PDUs per code, i.e., a $\gamma_i(t) = 2$ means that at time t , user i can transmit two PDUs using one code and up to 30 PDUs when using all the 15 codes. The Markov transition probability $P_{\gamma_i \gamma'_i}$ is known and can be calculated for any mobile environment with Rayleigh fading channel [8].

3.3 State and Action Sets

The system state $\mathbf{s}(t) \in S$ is a vector comprised of multiple state variables representing the queue sizes and the channel states for the L users. In other word,

$$\mathbf{s}(t) = (x_1(t), x_2(t), \dots, x_L(t), \gamma_1(t), \gamma_2(t), \dots, \gamma_L(t)) \quad (1)$$

and, $S = \{\mathcal{X} \times \mathcal{M}\}^L$ is finite, due to the assumption of finite buffers size and channel states.

The action space A is the set of all possible actions. The action $\mathbf{a}(\mathbf{s}) \in A$ is taken when in state \mathbf{s} . The action taken at each slot corresponds to the number of codes allocated to each user. Let $D = \{0, 1, \dots, 15/c\}$ be the

action space for a single user, where c is the code chunk size (the minimum number of codes that can be allocated at any given time). Let $a_i(\mathbf{s}) \in D$ be the number of code chunks allocated to user i when in state \mathbf{s} . Then the number of codes allocated to user i is $a_i(t)c$. In this case, $\mathbf{a}(\mathbf{s})$ will be the collection of code allocation to all users, that is

$$\mathbf{a}(\mathbf{s}) = (a_1(\mathbf{s}), a_2(\mathbf{s}), \dots, a_L(\mathbf{s})) \quad (2)$$

subject to

$$\sum_{i=1}^L a_i(\mathbf{s}) \leq \frac{15}{c}, \quad \text{and} \quad a_i(\mathbf{s}) \leq \left\lceil \frac{x_i(t)}{\gamma_i(t)c} \right\rceil$$

The first constraint means that the policy can not allocate more than the available 15 codes at each time slot. The second makes the policy conserving by allocating no more codes to user i than that required to empty its buffer.

3.4 Reward Function

In this subsection, we describe the reward function used to determine the optimal allocation policy. As stated previously, the objective is to maximize the throughput while maintaining fairness between active users. Let the *fairness factor*, denoted by σ , be a parameter that reflects the significance of fairness in the optimal policy. Define \bar{x} as the average instantaneous size of the L queues in the system at time t , i.e., $\bar{x} = \frac{1}{L} \sum_{i=1}^L x_i$, (we suppressed the time index to simplify notation). The reward function $R(\mathbf{s}, \mathbf{a})$ will have two components corresponding to the two objectives and it is given by

$$\begin{aligned} R(\mathbf{s}, \mathbf{a}) &= \sum_{i=1}^L y_i - \sigma \sum_{i=1}^L (x_i - \bar{x}) \mathbf{1}_{\{x_i=B\}} \\ &= \sum_{i=1}^L a_i \gamma_i c - \sigma \sum_{i=1}^L (B - \bar{x}) \mathbf{1}_{\{x_i=B\}} \end{aligned} \quad (3)$$

where $\mathbf{1}_{\{\cdot\}}$ is the indicator function. The positive term of the reward maximizes the cell throughput. If the reward is composed of this part only, then the policy will always favour the users with good channel conditions. Therefore the users with less favourable channels will starve. That is why we introduced the second term, which guarantees some level of fairness and reduces dropping probability. Lower σ will result in a policy that favours

cell throughput over fairness, while higher σ has the opposite effect. Overall, $R(\mathbf{s}, \mathbf{a})$ will produce a policy that maximizes cell throughput for a given σ .

3.5 Transition Probability function

$P_{ss'}(\mathbf{a})$ denotes the probability that choosing an action \mathbf{a} at time t when in state \mathbf{s} will lead to state \mathbf{s}' at time $t + 1$. Using (1) and (2), $P_{ss'}(\mathbf{a})$ can be stated as follows

$$\begin{aligned} P_{ss'}(\mathbf{a}) &= Pr(\mathbf{s}(t+1) = \mathbf{s}' | \mathbf{s}(t) = \mathbf{s}, \mathbf{a}(t) = \mathbf{a}) \\ &= Pr(x'_1, \dots, x'_L, \gamma'_1, \dots, \gamma'_L | x_1, \dots, x_L, \\ &\quad \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \end{aligned} \quad (4)$$

The evolution of the queue size (x_i) is given by

$$\begin{aligned} x'_i &= \min([x_i - y_i]^+ + z'_i, B) \\ &= \min([x_i - a_i \gamma_i c]^+ + z'_i, B) \end{aligned} \quad (5)$$

where, z'_i is the arrival to queue i at $t + 1$, $[e]^+$ equals e if $e \geq 0$ and 0 otherwise. The channel state γ_i depends only on the previous channel state, that is $Pr(\gamma'_i | \mathbf{s}) = Pr(\gamma'_i | \gamma_i) = P_{\gamma_i \gamma'_i}$. Accordingly, we can write (4) as follows (see Appendix A)

$$P_{ss'}(\mathbf{a}) = \prod_{i=1}^L (P_{x_i x'_i}(\gamma_i, a_i) P_{\gamma_i \gamma'_i}) \quad (6)$$

where $P_{\gamma_i \gamma'_i}$ is the Markov transition probability of the FSMC. Define $W1$ and $W2$ as follows

$$\begin{aligned} W1 &= [x_i - a_i \gamma_i c]^+ + u_i \\ W2 &= [x_i - a_i \gamma_i c]^+ \end{aligned}$$

We derived $P_{x_i x'_i}(\gamma_i, a_i)$ using (5) and the law of total probability (see Appendix B), and arrived at the following expression

$$P_{x_i x'_i}(\gamma_i, a_i) = \begin{cases} 1 & \text{if } x'_i = x_i = B \text{ \& } a_i \gamma_i = 0, \\ q_i & \text{if } x'_i = x_i = B \text{ \& } 0 < a_i \gamma_i c \leq u_i, \\ q_i & \text{if } x'_i = B \text{ \& } x_i < B \text{ \& } W1 \geq B, \\ q_i & \text{if } x'_i < B \text{ \& } x_i = W1, \\ 1 - q_i & \text{if } x'_i < B \text{ \& } x_i = W2, \\ 0 & \text{otherwise.} \end{cases} \quad (7)$$

The first three cases in (7) corresponds to the boundary state, while the remaining cases correspond to the non-boundary states.

3.6 Value Function

In this work, we investigate an infinite-horizon MDP. We use the total expected discounted reward optimality criterion with discount factor λ , where $0 < \lambda < 1$, in attempt to find the policy π among all policies, that maximize the *value function* $V^\pi(s)$. The following optimality equation is used to characterize the optimal policy

$$V^*(\mathbf{s}) = \max_{\mathbf{a} \in A} [R(\mathbf{s}, \mathbf{a}) + \lambda \sum_{\mathbf{s}' \in S} P_{\mathbf{s}\mathbf{s}'}(\mathbf{a}) V^*(\mathbf{s}')] \quad (8)$$

where $V^*(\mathbf{s})$ is the maximal discounted value function (i.e., $V^*(\mathbf{s}) = \sup_{\pi} V^\pi(\mathbf{s})$), attained when applying the optimal policy π^* .

Value iteration (also known as successive approximation) is used to solve this model numerically. The first step is to define $V_0(\mathbf{s})$ to be any arbitrary bounded function. Then run the following recursive equation for $n > 0$

$$V_n(\mathbf{s}) = \max_{\mathbf{a} \in A} [R(\mathbf{s}, \mathbf{a}) + \lambda \sum_{\mathbf{s}' \in S} P_{\mathbf{s}\mathbf{s}'}(\mathbf{a}) V_{n-1}(\mathbf{s}')] \quad (9)$$

V_n converges to V^* as $n \rightarrow \infty$ [12]. For a given $\epsilon > 0$, the algorithm can be stopped after n iteration, providing the following

$$\|V_{n+1} - V_n\| < \epsilon(1 - \lambda)/2\lambda \quad (9)$$

where $\|v\| = \sup_{s \in S} |v(s)|$. If (9) holds, then $\|V_{n+1} - V^*\| < \epsilon/2$, according to [9].

Using results from the discounted case we can generalize for the infinite horizon average reward using results from [9] and [12].

4 Two Users with 2-State FSMC

The approach presented earlier was used to model the case when there are two users (i.e., $L = 2$) sharing the same cell. The channel is modelled as a two-state FSMC with transition probability matrix

$$\begin{bmatrix} 1 - \alpha_i & \alpha_i \\ \beta_i & 1 - \beta_i \end{bmatrix} \quad (10)$$

The two user case will simplify the resultant policy and makes it easy to visualize, evaluate, and to deduct conclusions for the optimal policy. It also serves as a verification for the proposed approach, since it may be possible to verify the results for such a case intuitively. The obtained results can then be generalized to more complex cases.

User i is said to be *connected* when $\gamma_i = 1$ with probability $P(\gamma_i = 1) = \alpha_i / (\alpha_i + \beta_i)$, and *not connected* ($\gamma_i = 0$) with probability $P(\gamma_i = 0) = \beta_i / (\alpha_i + \beta_i)$.

The remaining parameters were chosen as follows: $B = 25$, $\sigma = 0.5$, $\lambda = 0.95$, $\epsilon = 0.1$, and $c = 3, 5$ or 15 . The action space depends on the value of c . For example, if $c = 5$ then there are *four* possible actions for each user (i.e., $D = \{0, 1, 2, 3\}$) and $A = \{(0,0), (0,1), (0,2), (0,3), (1,0), (1,1), (1,2), (2,0), (2,1), (3,0)\}$, where $\mathbf{a} = (a_1, a_2)$ corresponds to $a_1 c$ codes assigned to user1 and $a_2 c$ codes assigned to user 2. Similarly, when $c = 15$ then there are *two* possible actions per user (i.e., $D = \{0, 1\}$) and when $c = 3$ then there are *six* possible actions per user (i.e., $D = \{0, 1, 2, 3, 4, 5\}$).

4.1 Optimal Policy Structure

The model is solved using value iteration to determine the optimal scheduling policy. The effect of the channel quality and arrival probability on the behaviour of the optimal policy was studied. Figures 3-5 provide general structure of the optimal policy for $c = 15, 5$, and 3 respectively.

4.1.1 Optimal Policy for Two Symmetrical Users

The optimal policy for two symmetrical users with the same channel characteristics ($\alpha_i = \beta_i = p$) for all $0 \leq p \leq 1$ and with $P(z_i = 5) = 0.5$ for all $i \in \{1, 2\}$ is shown in sub-figures 3-5(a). Only the case when the two users have $\gamma_i = 1$ is shown here, since the two users are competing for the system resources. The other three cases when one or both of them has $\gamma = 0$ resulted in a policy that assigns all the codes (required) to the connected user and nothing to the other. The optimal policy in this case can be described as follows: *divide the codes between the connected users in proportion to their queue length*. When $c = 15$, the action space will be reduced to $A = \{(0,0), (0,1), (1,0)\}$ and the policy will be equivalent to *serve the longest queue first (LQF)*, which makes intuitive sense and matches with the findings in [13] for a case similar to the $c = 15$ case.

4.1.2 The Effect of Channel Quality on Policy Structure

The effect of the channel quality on the optimal policy structure when $\gamma_1 = \gamma_2 = 1$ is shown in sub-figures 3-5(b). When $P(\gamma_1 = 1) > P(\gamma_2 = 1)$ the policy favours user 2 which is less likely to have $\gamma_2 = 1$ compared to user 1. The bias in favour of user 2 is depicted in sub-figures 3-5(b) by a larger dark area, which corresponds to optimal action (0,1), (0,3) or (0,5) respectively, compared to sub-figures 3-5(a). We noticed that this bias increases as the difference between $P(\gamma_1 = 1)$ and $P(\gamma_2 = 1)$ increases. The reason is that using an LQF in this situation will result in uncontrollable growth in user 2 queue. User 2 will start experiencing unfairness in terms of higher delay and more drops. Hence, more resources have to be assigned to the user with the worst channel to avoid that result. The resource sharing in this case will be governed by the difference $\Delta P_\gamma = P(\gamma_1 = 1) - P(\gamma_2 = 1)$ as well as their relative queue length.

4.1.3 The Effect of Arrival Probability on Policy Structure

The arrival probability has similar effect on the optimal policy structure. The relative increase in one of the users arrival probability will result in more traffic inserted in that user's buffer and it will require more resources to keep the queue length stable and achieve fairness between the two users.

Sub-figures 3-5(c) shows the optimal policy when $P(z_1 = 5) = 0.8$ and $P(z_2 = 5) = 0.5$ and both users have the same channel quality. The policy shifts in favour of the user with higher arrival probability (user 1 in this case). The shift is proportional to the difference $\Delta P_z = P(z_1 = u) - P(z_2 = u)$.

5 The Heuristic Policy

The optimal policy allocates the codes in proportion to the *weighted* queue length of the connected users. We devised a heuristic approach for code allocation in HSDPA system that works in the three cases introduced earlier (i.e., $c = 15, 5$ or 3) and takes into account the channel quality and load variations. It can also be used (with little modifications) for any value of c . The suggested heuristic policy tries to mimic the behaviour of the optimal policy studied in 4.

The weight (w_i) is a function of the difference of the two channel qualities

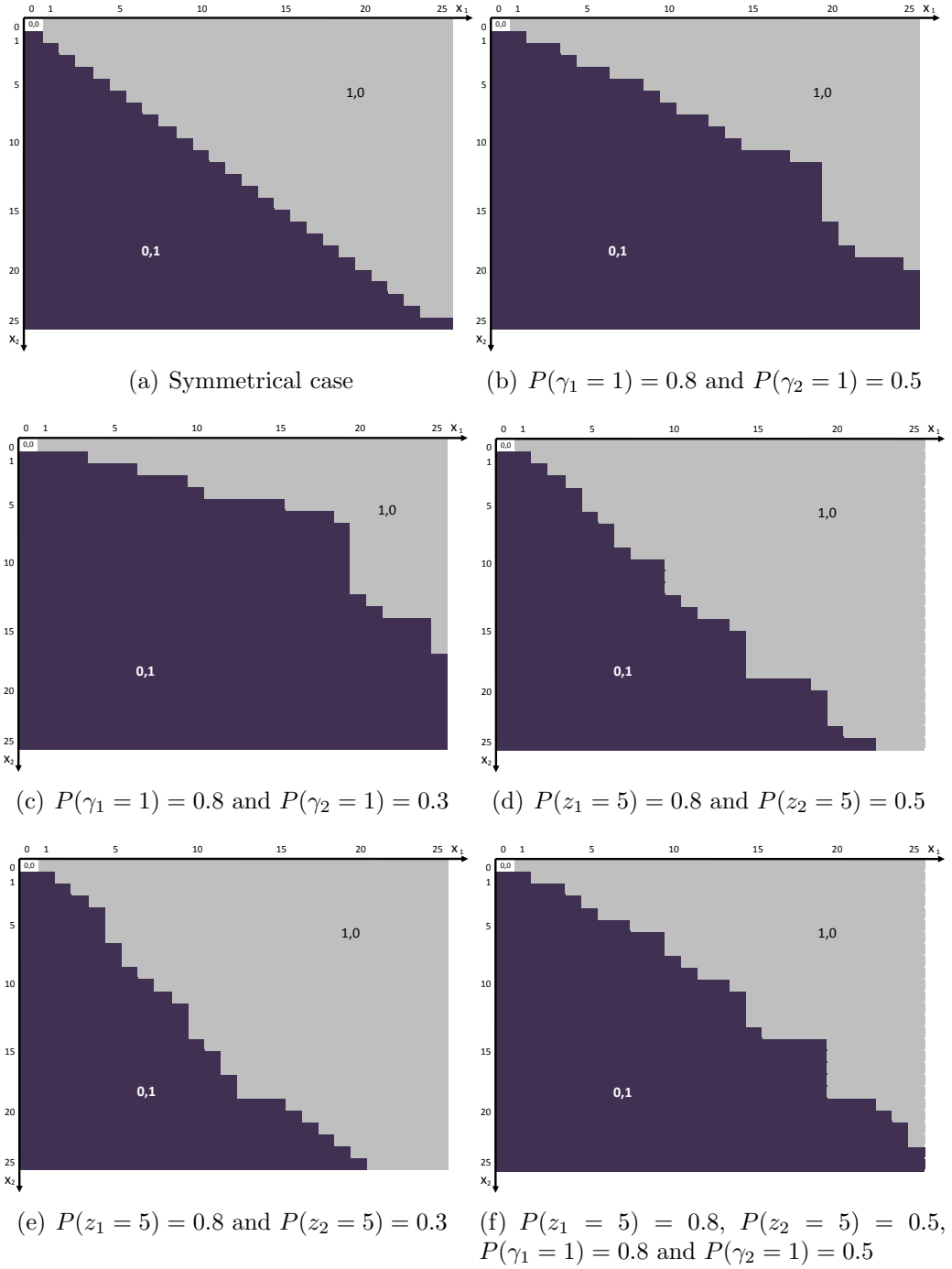


Figure 3: The optimal policy for two user case; $c = 15$

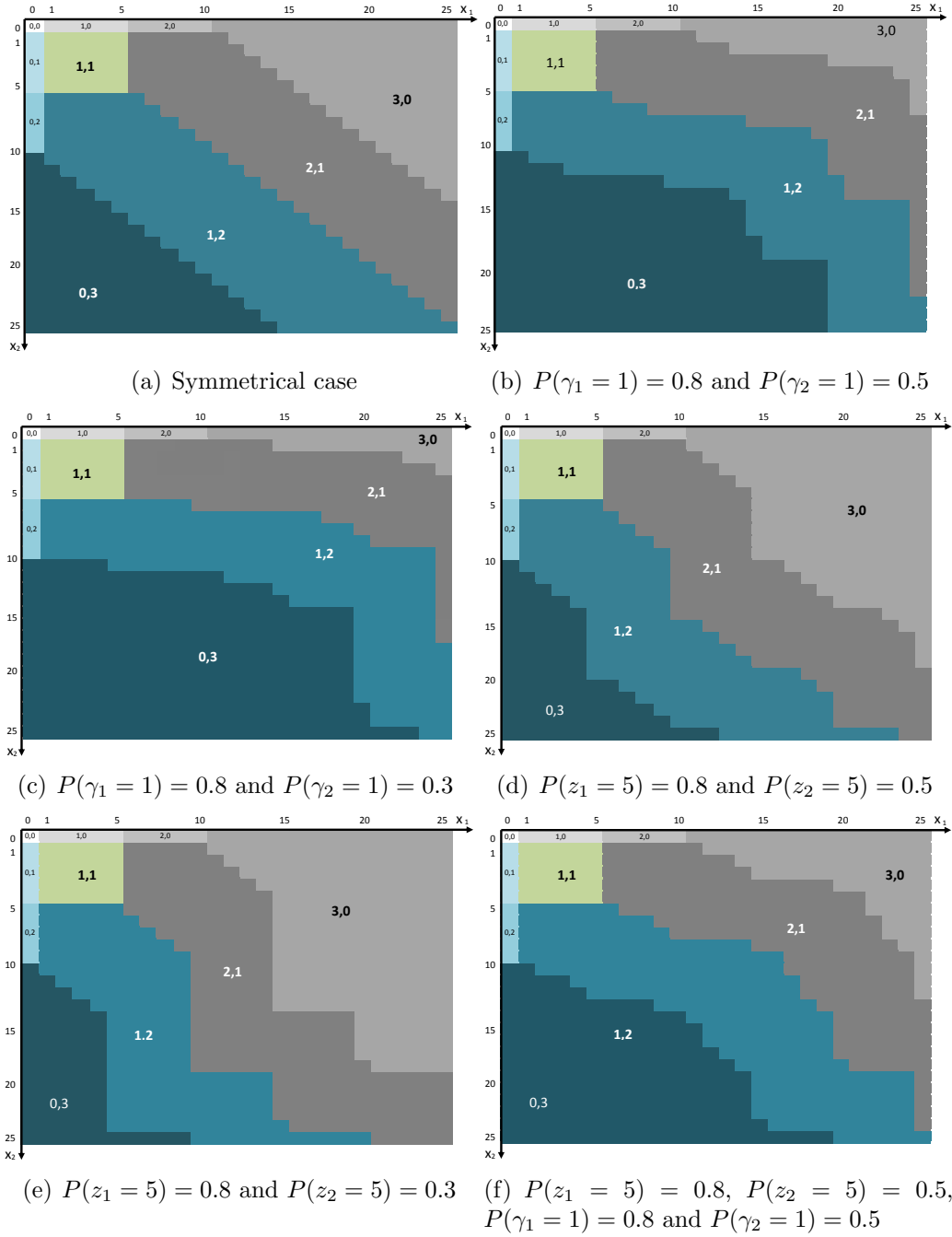


Figure 4: The optimal policy for two user case; $c = 5$

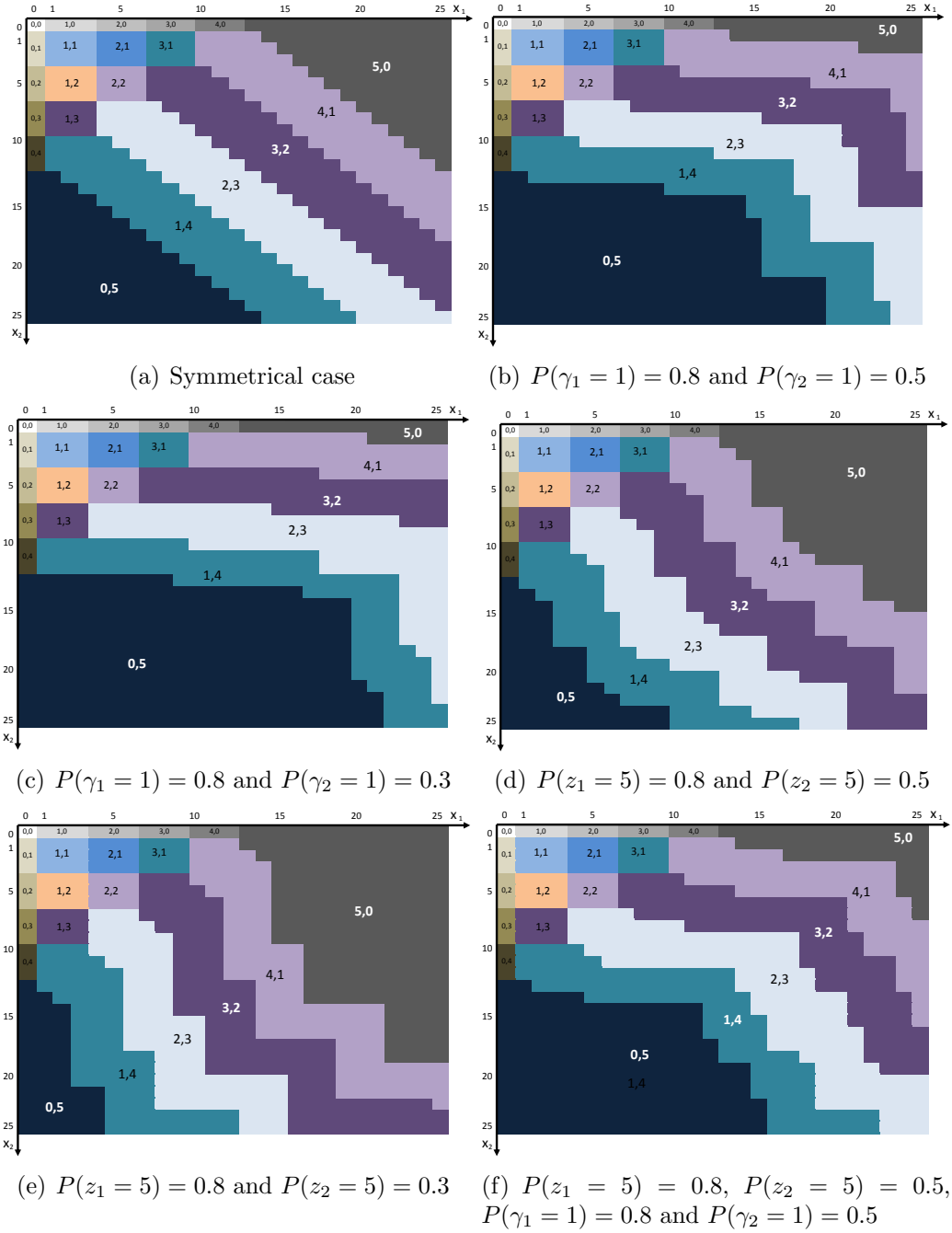


Figure 5: The optimal policy for two user case; $c = 3$

and that of the arrival probabilities:

$$w_1 = f([-ΔP_γ]^+, [-ΔP_z]^+) \quad (11)$$

$$w_2 = f([ΔP_γ]^+, [ΔP_z]^+) \quad (12)$$

5.1 Heuristic policy ($c = 15$)

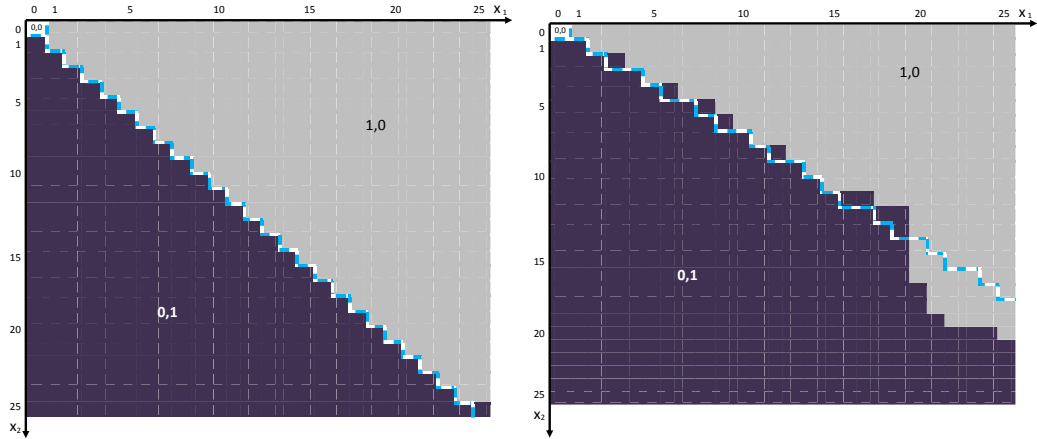
In this case, the optimal policy is a switch over policy as depicted in Figure 3. We can identify three regions which correspond to the three possible actions: (0,0), (1,0) and (0,1). The heuristic policy is a weighted LQF and it assigns codes to users according to the following rules:

- Rule1: when there is only one connected user then assign all the needed codes to that user,
- Rule2: when both users are not connected (i.e., $\gamma_1 = \gamma_2 = 0$) then no codes will be allocated to any user,
- Rule3: when the two users are connected allocate code chunks according to (13) below

$$\mathbf{a}(t) = \begin{cases} (1, 0) & \text{if } w_1x_1 > w_2x_2, \\ (0, 1) & \text{if } w_1x_1 \leq w_2x_2 \end{cases} \quad (13)$$

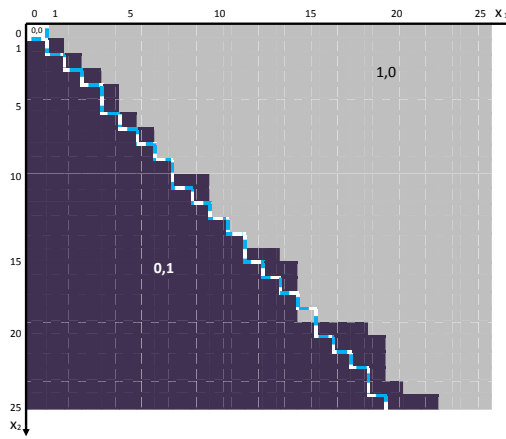
5.2 Heuristic Policy ($c = 5$)

The optimal policy defines ten each of which is characterized by an optimal action as shown in section 4. However, only four of these regions are of interest. They lie within the area where the demand exceeds the available resources as shown in Figure 4. Based on this observation, the heuristic policy partitions the state space into four major regions that corresponds to the actions (3,0), (2,1), (1,2), and (0,3). The heuristic policy defines two additional regions corresponds to actions (0,0) and (1,1) to make the policy conservative. The same heuristic policy in 5.1 above will apply here except for Rule3 which will be modified as follows:



(a) Symmetrical case

(b) $\Delta P_\gamma = 0.3, \Delta P_z = 0$



(c) $\Delta P_\gamma = 0, \Delta P_z = 0.3$

Figure 6: The heuristic policy (dotted line) in comparison to the optimal policy; $c = 15$

- Rule3: when the two users are connected, *if* $x_1 + x_2 < 15$ *then* allocate codes to the two users in proportion to their queue length, *else* allocate the code chunks as follows

$$\mathbf{a}(t) = \begin{cases} (3, 0) & \text{if } w_1x_1 > w_2x_2 + 10, \\ (2, 1) & \text{if } w_2x_2 < w_1x_1 \leq w_2x_2 + 10, \\ (1, 2) & \text{if } w_2x_2 - 10 \leq w_1x_1 \leq w_2x_2, \\ (0, 3) & \text{if } w_1x_1 < w_2x_2 - 10, \end{cases} \quad (14)$$

5.3 Heuristic Policy ($c = 3$)

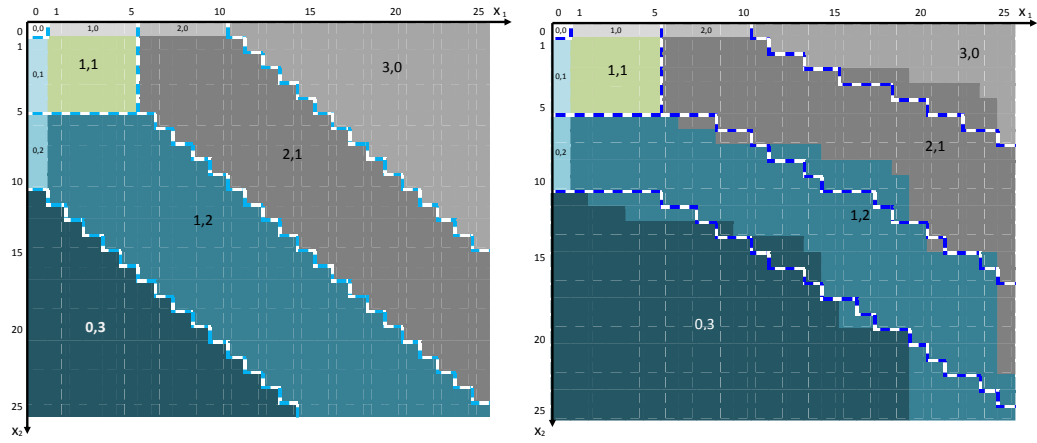
There are 21 different regions in the state space as shown in Figure 5. The heuristics used in 5.1 and 5.2 can be extended to this case. Again only Rule3 need to be modified as shown below

- Rule3: when the two users are connected, *if* $x_1 + x_2 < 15$ *then* allocate codes to the two users in proportion to their queue length, *else* allocate the code chunks as follows

$$\mathbf{a}(t) = \begin{cases} (5, 0) & \text{if } w_1x_1 > w_2x_2 + 12, \\ (4, 1) & \text{if } w_2x_2 + 6 < w_1x_1 \leq w_2x_2 + 12, \\ (3, 2) & \text{if } w_2x_2 < w_1x_1 \leq w_2x_2 + 6, \\ (2, 3) & \text{if } w_2x_2 - 6 < w_1x_1 \leq w_2x_2, \\ (1, 4) & \text{if } w_2x_2 - 12 < w_1x_1 \leq w_2x_2 - 6, \\ (0, 5) & \text{if } w_1x_1 \leq w_2x_2 - 12, \end{cases} \quad (15)$$

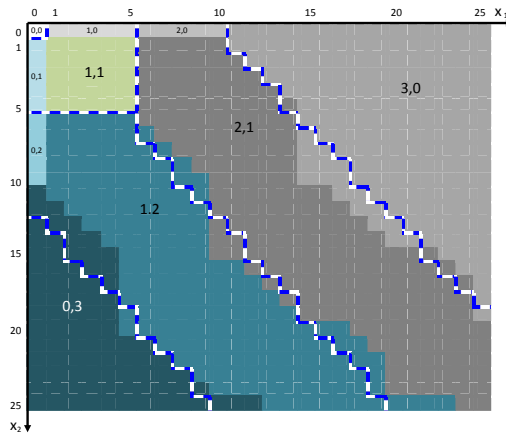
5.4 Weight Function and Other Considerations

We observed the behaviour of the optimal policy by running a range of scenarios. We noticed that the intermediate regions (e.g., the regions corresponds to actions (1,2) and (2,1) in ' $c = 5$ ' case) has almost a constant width that equals $2c$ in all the scenarios that have been studied. We also noticed that the optimal policy is monotonic and a_1 (respectively a_2) is increasing in x_1 (respectively x_2). It is also apparent from the studied scenarios that $f()$ is



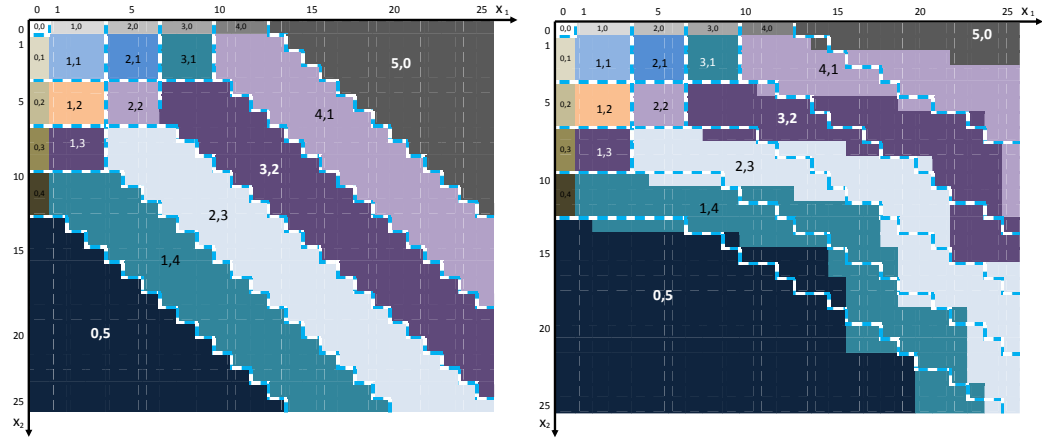
(a) Symmetrical case

(b) $\Delta P_\gamma = 0.3, \Delta P_z = 0$



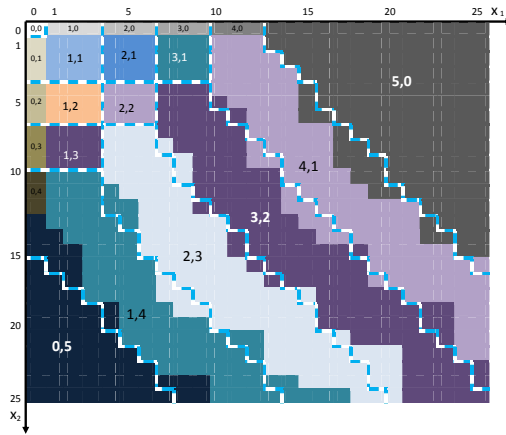
(c) $\Delta P_\gamma = 0, \Delta P_z = 0.3$

Figure 7: The heuristic policy (dotted line) in comparison to the optimal policy; $c = 5$



(a) Symmetrical case

(b) $\Delta P_\gamma = 0.3, \Delta P_z = 0$



(c) $\Delta P_\gamma = 0, \Delta P_z = 0.3$

Figure 8: The heuristic policy (dotted line) in comparison to the optimal policy; $c = 3$

increasing in $|\Delta P_\gamma|$ and decreasing in $|\Delta P_z|$. Following these observations, we approximated w_1 and w_2 as follows

$$\hat{w}_1 = 1 + 1.5[-\Delta P_\gamma]^+ - 0.7[-\Delta P_z]^+ \quad (16)$$

$$\hat{w}_2 = 1 + 1.5[\Delta P_\gamma]^+ - 0.7[\Delta P_z]^+ \quad (17)$$

The ratio w_1/w_2 represents the slope of the switchover line between the different areas in the policy. When $\Delta P_\gamma=0$ and $\Delta P_z=0$ then $\hat{w}_1/\hat{w}_2=1$ and the policy for the three cases will look exactly like the ones in sub-figures 3-5(a). The suggested heuristic policy can be modified to accommodate classes. This is done by adding a multiplicative parameter to the weight in (16) to implement differentiated services.

Figures 6-8 show the heuristic policy (the dotted line) superimposed on the optimal policy from section 4 for different loading and channel quality conditions. From these figures, it is fair to say that there is a reasonable convergence between the heuristic policy and the optimal policy.

We also noticed that the effect of σ is minimal in this case. This is mainly due to the two-states channel model (connected or not connected). When connected, both users will have the same data rate and serving either one will result in the same reward. However, it is expected that σ will have a prominent role when using FSMC model with more than two states.

6 Performance Evaluation

The performance of the optimal policy and the devised heuristic policy was studied using simulation. The Round Robin fair queueing is used as a baseline. All the assumptions made before is also used in the simulation for consistency. The buffers sizes used in this part is $B_1 = B_2 = 50$.

6.1 The Effect of Policy Granularity

The number of available codes to be allocated at one TTI is 15 codes according to 3GPP [1]. We define the *policy granularity* to be a measure of how fine/coarse is the code allocation during one TTI. It has a direct relation to the chunk size c . It ranges from finest ($c = 1$), then the policy can assign as little as 1 code to a user at a time, to the coarsest ($c = 15$), then all the 15 codes can be assigned to one user only at a time. Figures 9-12 show the effect of policy granularity on system performance for different ρ .

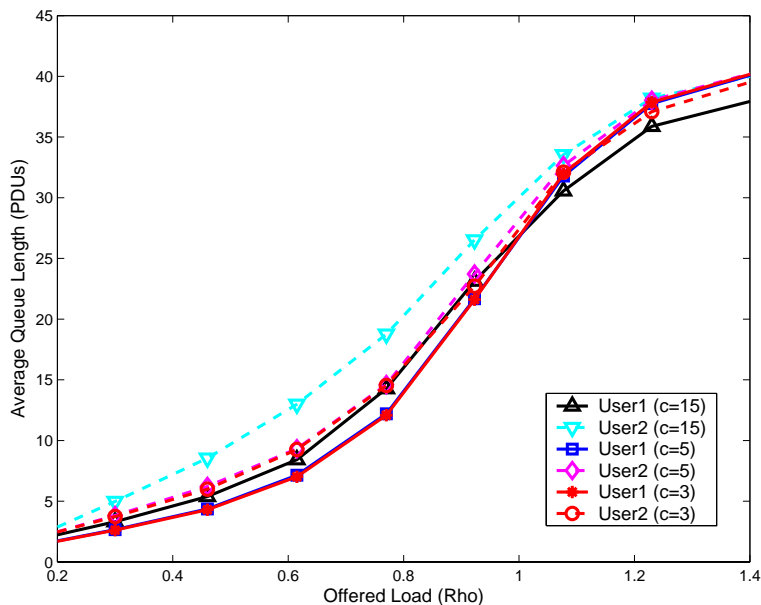


Figure 9: The effect of policy granularity on queue length

Where $\rho = \sum_i P_{z_i} u_i / r^\pi$ is the offered load and r^π is the measured system capacity under the policy π . We selected the channel state probabilities to be $P(\gamma_1 = 1) = 0.84$ and $P(\gamma_2 = 1) = 0.5$. Using (10), The channel model parameters (α_i and β_i) were calculated.

The results show that in light and moderate load conditions ($\rho \ll 1$), the average queue length is shorter when using finer granularity. However, when $\rho \rightarrow 1$ the difference start diminishing and eventually reversed when ρ becomes greater or equal to 1. It is known that shorter queue length means shorter delay and better QoS and scheduler performance.

Another valuable observation is that the performance gain when moving from $c = 5$ to $c = 3$ is only marginal and does not justify the added implementation and computational complexity. It is noteworthy that in heavy load and overload conditions, a coarse policy ($c = 15$) performs better than a finer one. This is true for the 2 state FSMC model case and we do not expect it to hold for higher number of states.

It is interesting to see that the optimal policy under all of the three values of c achieved approximately the same throughput (see Figure 11). The slight throughput loss when $c = 15$ in moderate to high load is due to the increased

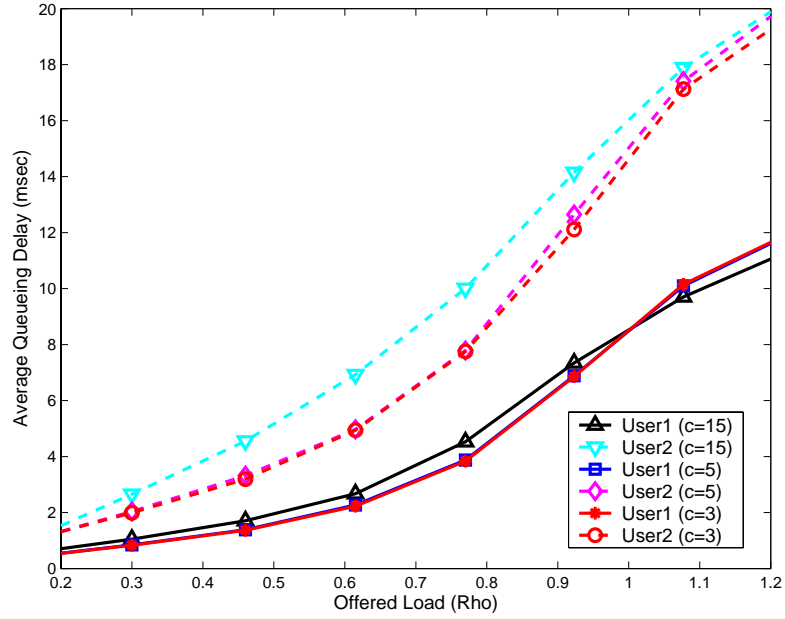


Figure 10: The effect of policy granularity on the average queuing delay experienced by the two users

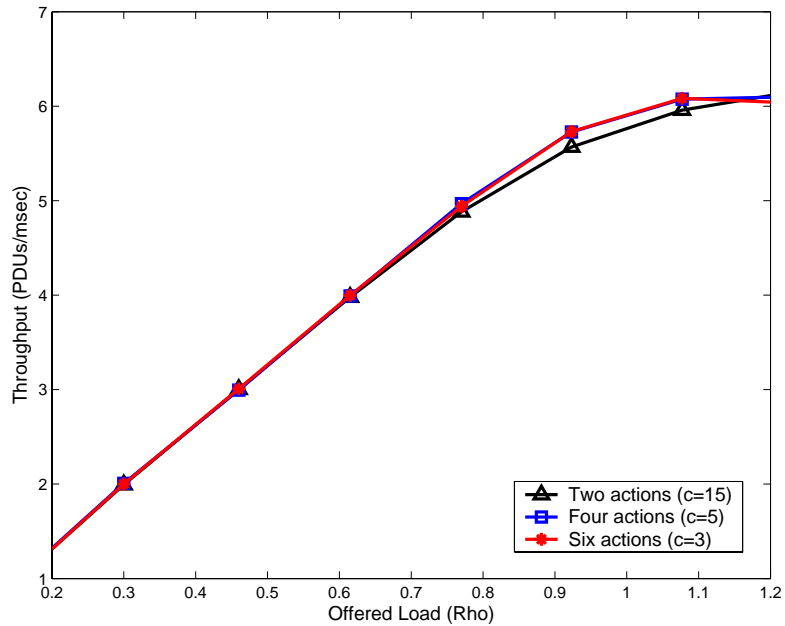


Figure 11: The effect of policy granularity on scheduler throughput

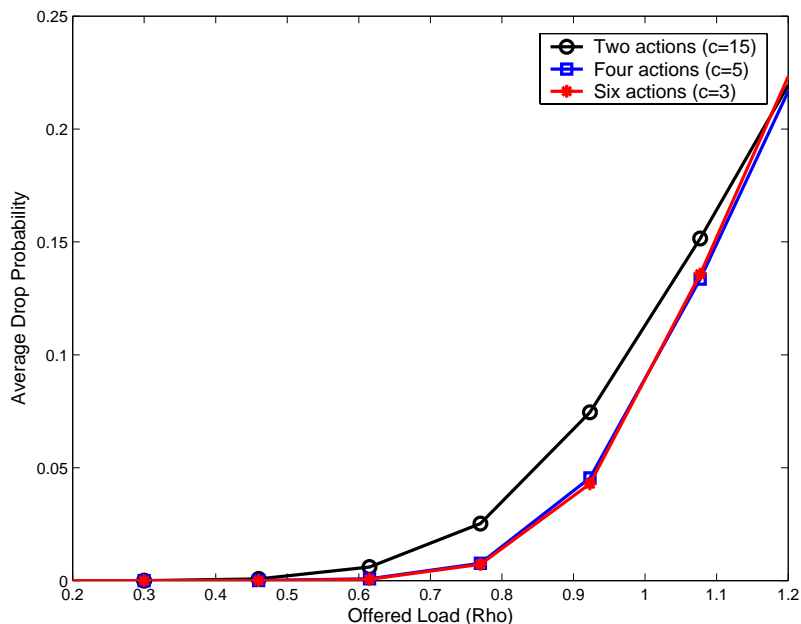


Figure 12: The effect of policy granularity on scheduler dropping probability

drops at these particular conditions as it is shown in Figure 12. The reason for the increased dropping probability in this case can be explained by the fact that serving only one user at a time, which is the case when $c = 15$, will increase the probability that the other user will have a buffer overflow. While in the other two cases both users can be served at the same time by dividing the code chunks between them. Such behaviour will reduce the chance of buffer overflow.

6.2 Heuristic Policy Evaluation

The system throughput when applying the heuristic policy is shown in Figure 13. The cases when using Round Robin and the optimal policy are also shown for comparison. The channel model parameters was chosen such that $P(\gamma_1 = 1) = 0.84$ and $P(\gamma_2 = 1) = 0.5$. Figure 13 shows that the suggested heuristic policy performs very close to the optimal policy. It also shows that RR performance converges to that of the optimal policy in case of light loading (e.g., $\rho = 0.5$). However, it performs 30% worse than the optimal policy in heavy load conditions when $\rho = 1.2$. Where $\rho = \sum_i P_{z_i} u_i / r^\pi$ is the offered load and r^π is the measured system capacity under the policy π .

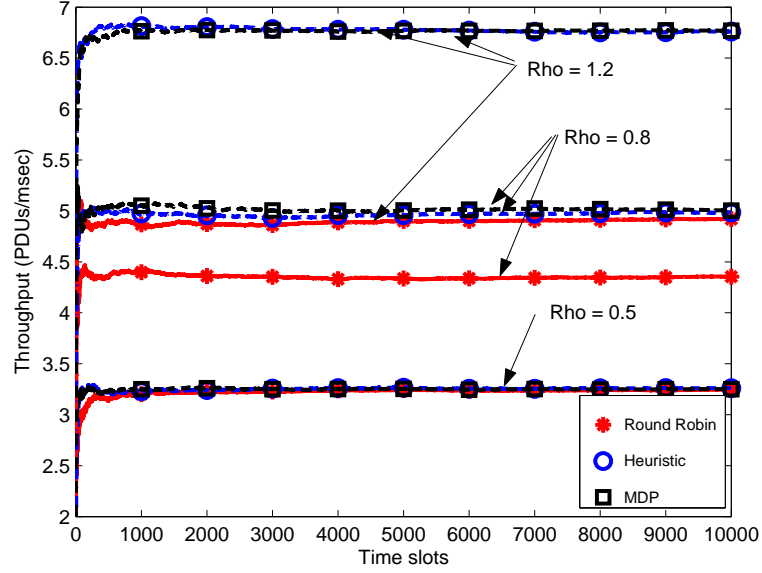


Figure 13: System throughput for different loading conditions.

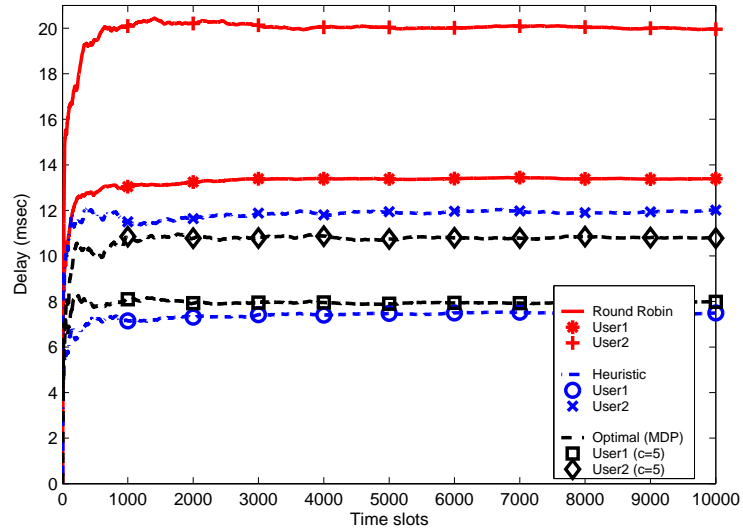


Figure 14: Queuing delay performance, $P(\gamma_1 = 1) = 0.84$, $P(\gamma_2 = 1) = 0.5$, $q_1 = 0.8$, $q_2 = 0.5$ and $u = 10$.

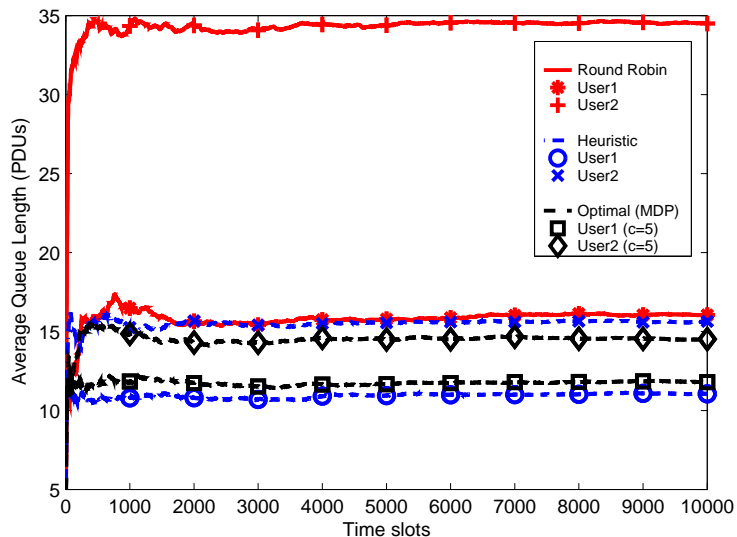


Figure 15: Queue length, $\rho = 0.75$, $P(\gamma_1 = 1) = 0.84$, $P(\gamma_2 = 1) = 0.5$, $q_1 = 0.5$, $q_2 = 0.5$ and $u = 10$.

Queueing delay performance is shown in Figure 14. Figures 15 and 17 show the average queue lengths of both users for the suggested heuristic policy in comparison with that of RR and the optimal policy. From those graphs, the following conclusions were deduced:

- The proposed heuristic policy performance is very close to that of the optimal policy.
- The optimal policy provides the smallest difference in queueing delay between the two users, which means higher fairness level. The heuristic policy provides a comparable performance to that of the optimal policy, while the round robin has the worst fairness and delay performance.
- The performance of the RR policy is highly dependent on the loading conditions. The results obtained proved that RR has poor performance in wireless channel.

The reason why RR performs so poorly in wireless environment is that it does not take into account the channel quality variation, while the optimal policy tracks this variation very closely.

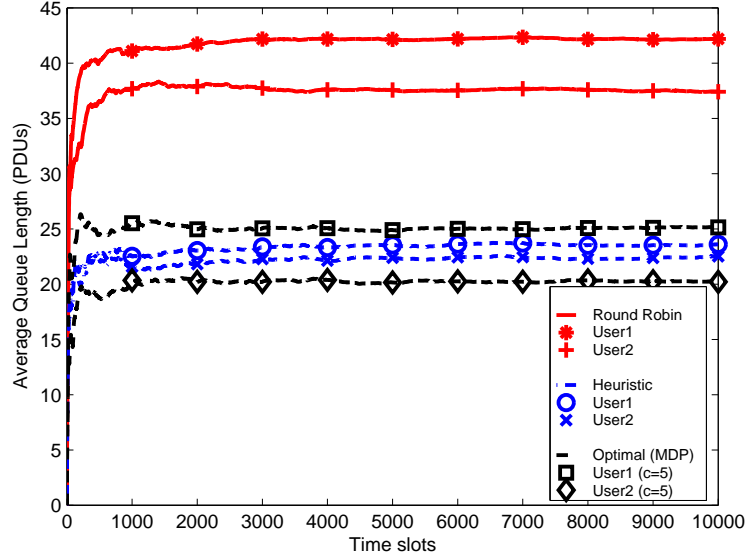


Figure 16: Queue length, $\rho = 1.0$, $P(\gamma_1 = 1) = 0.84$, $P(\gamma_2 = 1) = 0.5$, $q_1 = 0.8$, $q_2 = 0.5$ and $u = 10$.

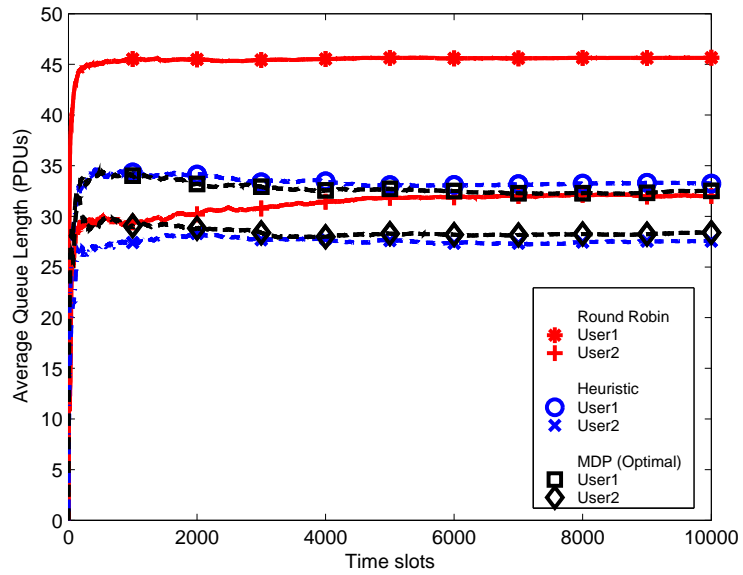


Figure 17: Queue length, $\rho = 1.1$, $P(\gamma_1 = 1) = 0.6$, $P(\gamma_2 = 1) = 0.6$, $q_1 = 0.8$, $q_2 = 0.5$ and $u = 10$.

6.3 Computational Complexity

The approach used is to run the value iteration for a system with small B , to reduce the computation time, then use this model to study the structure of the optimal policy for different channel conditions and loading scenarios. The obtained information is then used to build a heuristic policy that can be expanded to larger buffers sizes. The same approach can be used in the case when more than two users are involved.

The suggested heuristic approach trades performance for simplicity. However, the small performance loss is acceptable price to pay for the huge reduction in computation time. The policy determination using the heuristic approach can be calculated instantly. On the other hand, it took the value iteration about 6 hours to converge when $c = 5$ and $B = 50$.

The heuristic policy has deterministic polynomial complexity with constant time complexity, i.e., $O(1)$. On the other hand, the calculation of the optimal policy has an exponential time complexity in B with $O(B^L)$ per one iteration, where L is the number of active users in the system, and is intractable for very large B . The number of iteration required depends on how fast the policy converges, which in turn depends on many other parameters, such as ϵ , λ , and c . Studying the exact complexity for this problem is out of the scope of this report.

7 Conclusion

An MDP model for the scheduling problem in 3G-HSDPA wireless system was developed. Value iteration was used to solve for the optimal scheduling policy for a system with two users and two-states Finite State Markov Channel model. The policy structure was obtained for different policy granularities. The study showed that the optimal policy can be described as *share the codes in proportion to the weighted queue length of the connected users*.

The effect of the granularity on the optimal policy performance in the two users and two-states FSMC case was studied. It also showed that a policy with finer granularity will perform better in light to moderate loading conditions, while a coarse policy is more desirable in heavy loading conditions. However, the performance gain when using $c < 5$ is marginal and does not justify the added complexity.

We developed a heuristic approach to obtain a near-optimal policy. It has a reduced constant time complexity ($O(1)$) as compared to the exponential time complexity needed in the determination of the optimal policy. The suggested approach involves studying the behavioural characteristics of the optimal policy using the MDP model for small buffer size. Then use this data to determine a generalized near-optimal heuristic scheduling policy. The performance of the resulted heuristic policy matches very closely to the optimal policy. The results also proved that RR is undesirable in HSDPA system due to the poor performance and lack of fairness if deployed in such environment. The suggested heuristic policy can be extended to the case with more than two active users. It also can be easily adapted to accommodate more than one class of service.

APPENDIX A

State Transition Probability

To derive the state transition probability ($P_{ss'(\mathbf{a})}$) that was introduced in section 3, we start from equation (4) as follows

$$\begin{aligned} P'_{ss'}(\mathbf{a}) &= Pr(\mathbf{s}(t+1) = \mathbf{s}' | \mathbf{s}(t) = \mathbf{s}, \mathbf{a}(t) = \mathbf{a}) \\ &= Pr(x'_1, \dots, x'_L, \gamma'_1, \dots, \gamma'_L | x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \end{aligned} \quad (\text{A-1})$$

Using Bayes' theorem we can decompose the above joint probability as follows

$$\begin{aligned} P_{ss'}(\mathbf{a}) &= Pr(x'_1, \dots, x'_L | x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \cdot \\ &\quad Pr(\gamma'_1, \dots, \gamma'_L | x'_1, \dots, x'_L, x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \end{aligned} \quad (\text{A-2})$$

Using Bayes' theorem again to decompose the second part of (A-2)

$$\begin{aligned} P_{ss'}(\mathbf{a}) &= Pr(x'_1, \dots, x'_L | x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \cdot \\ &\quad Pr(\gamma'_1 | x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \cdot \\ &\quad Pr(\gamma'_2 | \gamma'_1, x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \dots \\ &\quad Pr(\gamma'_L | \gamma'_1, \dots, \gamma'_{L-1}, x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \end{aligned} \quad (\text{A-3})$$

Since the wireless channel was modelled by a birth and death process, and because of the memoryless property of Markov processes, the channel state γ_i depends only on the previous channel state and is independent of everything else. Hence, The channel state transition probability is given by

$$Pr(\gamma'_i | \mathbf{s}) = Pr(\gamma'_i | \gamma_i) = P_{\gamma_i \gamma'_i}$$

Accordingly, we can rewrite (A-3) as follows

$$P_{ss'}(\mathbf{a}) = Pr(x'_1, \dots, x'_L | x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \cdot \prod_{i=1}^L P_{\gamma_i \gamma'_i} \quad (\text{A-4})$$

Using the same technique, the joint probability of the queue size can be decomposed as follows

$$\begin{aligned} &Pr(x'_1, \dots, x'_L | x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \\ &= Pr(x'_1 | x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \cdot \\ &\quad Pr(x'_2 | x'_1, x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \dots \\ &\quad Pr(x'_L | x'_1, \dots, x'_{L-1}, x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \end{aligned} \quad (\text{A-5})$$

The evolution of the queue size (x_i) is given by

$$\begin{aligned} x'_i &= \min([x_i - y_i]^+ + z'_i, B) \\ &= \min([x_i - a_i \gamma_i c]^+ + z'_i, B) \end{aligned} \tag{A-6}$$

It is obvious that the queue size at the next slot (x'_i) depends on the current queue size (x_i), the serviced PDUs y_i at time t and the arrived PDUs z'_i during $(t, t + 1]$ for user i and independent on anything else. Hence

$$Pr(x'_i | \mathbf{s}) = Pr(x'_i | x_i, \gamma_i, a_i) = P_{x_i x'_i}(\gamma_i, a_i)$$

and equation (A-5) will be reduced to

$$P_{ss'}(\mathbf{a}) = \prod_{i=1}^L (P_{x_i x'_i}(\gamma_i, a_i) P_{\gamma_i \gamma'_i}) \tag{A-7}$$

The state transition probability will be the product of the individual users' queue state transition probabilities and their FSMC channel transition probabilities. The underline assumption is that $P_{\gamma_i \gamma'_i}$ is measurable and known for the scheduler. However, $P_{x_i x'_i}(\gamma_i, a_i)$ has to be determined. In APPENDIX B we will find queue state transition probability and derive an expression for this probability.

APPENDIX B

Queue State Transition Probability

The queue size evolves according to

$$x_i(t+1) = \min([x_i(t) - y_i(t)]^+ + z_i(t+1), B) \quad (\text{B-1})$$

where $y_i(t) = a_i(t)\gamma_i(t)c$.

The queue transition probability is given by

$$P_{x_i x'_i}(\gamma_i, a_i) = Pr(x_i(t+1) = x'_i | x_i(t) = x_i, \gamma_i(t) = \gamma_i, a_i(t) = a_i) \quad (\text{B-2})$$

Substituting (B-1) in (B-2) yields the following

1. when $[x_i(t) - y_i(t)]^+ + z_i(t+1) < B$ then

$$x_i(t+1) = [x_i(t) - y_i(t)]^+ + z_i(t+1)$$

and

$$\begin{aligned} P_{x_i x'_i}(\gamma_i, a_i) &= Pr([x_i(t) - y_i(t)]^+ + z_i(t+1) = x'_i | x_i(t) = x_i, \\ &\quad \gamma_i(t) = \gamma_i, a_i(t) = a_i) \\ &= Pr([x_i - y_i]^+ + z_i(t+1) = x'_i) \end{aligned} \quad (\text{B-3})$$

Then $P_{x_i x'_i}(\gamma_i, a_i)$ is related to the arrival probability as follows

$$P_{x_i x'_i}(\gamma_i, a_i) = Pr(z_i(t+1) = x'_i - [x_i - y_i]^+) \quad (\text{B-4})$$

The arrival process is assumed to be Bernoulli with parameter q_i for user i and is given by

$$z_i(t) = \begin{cases} u_i & \text{with probability } q_i \\ 0 & \text{with probability } 1 - q_i \end{cases} \quad (\text{B-5})$$

Hence, the queue state transition probability in this case will be

$$P_{x_i x'_i}(\gamma_i, a_i) = \begin{cases} q_i & \text{if } x'_i = [x_i - y_i]^+ + u_i \\ 1 - q_i & \text{if } x'_i = [x_i - y_i]^+ \\ 0 & \text{Otherwise} \end{cases} \quad (\text{B-6})$$

2. when $[x_i(t) - y_i(t)]^+ + z_i(t+1) \geq B$ then $x_i(t+1) = B$ and

$$\begin{aligned} P_{x_i B}(\gamma_i, a_i) &= Pr([x_i(t) - y_i(t)]^+ + z_i(t+1) \geq B | x_i(t) = x_i, \\ &\quad \gamma_i(t) = \gamma_i, a_i(t) = a_i) \\ &= Pr([x_i - y_i]^+ + z_i(t+1) \geq B) \end{aligned} \quad (\text{B-7})$$

The above equation can be written as follows

$$P_{x_i B}(\gamma_i, a_i) = Pr(z_i(t+1) \geq B - [x_i - y_i]^+) \quad (\text{B-8})$$

which is the queue transition probability in terms of the arrival probability. Using (B-5) and (B-8), we can write $P_{x_i B}(\gamma_i, a_i)$ as follows

$$P_{x_i B}(\gamma_i, a_i) = \begin{cases} q_i & \text{if } [x_i - y_i]^+ + u_i \geq B \\ 1 - q_i & \text{if } [x_i - y_i]^+ \geq B \\ 0 & \text{Otherwise} \end{cases} \quad (\text{B-9})$$

Substituting for y_i in B-9 yields

$$P_{x_i B}(\gamma_i, a_i) = \begin{cases} q_i & \text{if } [x_i - \gamma_i a_i c]^+ + u_i \geq B \\ 1 - q_i & \text{if } [x_i - \gamma_i a_i c]^+ \geq B \\ 0 & \text{Otherwise} \end{cases} \quad (\text{B-10})$$

Using our knowledge of queue evolution process, we can summarize all the possible transitions in (B-10) by

$$P_{x_i B}(\gamma_i, a_i) = \begin{cases} 1 & \text{if } x'_i = x_i = B \ \& \ \gamma_i a_i = 0 \\ q_i & \text{if } x'_i = x_i = B \ \& \ 0 < \gamma_i a_i c \leq u_i \\ q_i & \text{if } x'_i = B \ \& \ x_i < B \ \& \ [x_i - \gamma_i a_i c]^+ + u_i \geq B \\ 0 & \text{Otherwise} \end{cases} \quad (\text{B-11})$$

The results obtained above in (B-6) and (B-11) can be summarized as follows

$$P_{x_i B}(\gamma_i, a_i) = \begin{cases} 1 & \text{if } x'_i = x_i = B \ \& \ \gamma_i a_i = 0 \\ q_i & \text{if } x'_i = x_i = B \ \& \ 0 < \gamma_i a_i c \leq u_i \\ q_i & \text{if } x'_i = B \ \& \ x_i < B \ \& \ [x_i - \gamma_i a_i c]^+ + u_i \geq B \\ q_i & \text{if } x'_i < B \ \& \ x'_i = [x_i - \gamma_i a_i c]^+ + u_i \\ 1 - q_i & \text{if } x'_i < B \ \& \ x'_i = [x_i - \gamma_i a_i c]^+ \\ 0 & \text{Otherwise} \end{cases} \quad (\text{B-12})$$

APPENDIX C

Service Rate Estimation in Case of Two Users Sharing A Server

In This Appendix we will derive an expression that relates the required server share of each user to the probability of its channel connectivity in a two user system with one shared server. The embedded assumption that the two users have equal arrival rate that is large enough to keep large queue occupancy all the time. The system is modelled by two queues as shown in Figure 18. The two queues are connected with probabilities π_1 and π_2 respectively. There

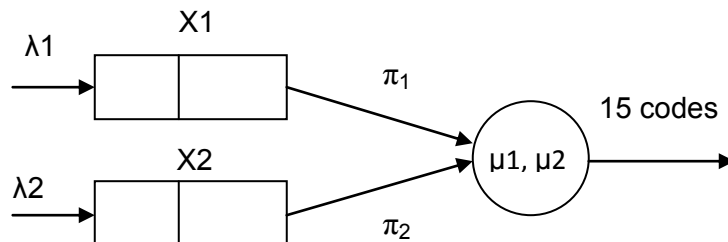


Figure 18: Two queue model with shared server and random channel connectivity

are 15 codes to be shared between the two users when both are connected. Each code is good to serve one packet. When only one queue is connected then all the 15 codes will be assigned to the connected one. The service rates for queue 1 and queue 2 are μ_1 and μ_2 respectively. The service rates for the two queues are determined in the following,

- **Service rate for queue 1:** Queue 1 can be served only if user 1 is connected. When user 1 is connected and user 2 is not then the 15 codes will be assigned to serve queue 1. This happens with probability $\pi_1(1 - \pi_2)$. when both are connected then both will share the server according to the adapted scheduling policy. This happens with probability $\pi_1\pi_2$. Hence, the average service rate for queue 1 is given by,

$$\begin{aligned} \mu_1 &= 15\pi_1(1 - \pi_2) + 15m_1\pi_1\pi_2 && \text{packets per second} \\ &= 15\pi_1(1 - \pi_2(1 - m_1)) && \text{(C-1)} \end{aligned}$$

- **Service rate for queue 2:** Same argument is valid for queue 2. Average service rate for queue 2 is given by,

$$\begin{aligned}\mu_2 &= 15\pi_2(1 - \pi_1) + 15m_2\pi_1\pi_2 && \text{packets per second} \\ &= 15\pi_2(1 - \pi_1(1 - m_2))\end{aligned}\tag{C-2}$$

where m_1 and m_2 are the portions of the server assigned to serve queue 1 and queue 2 respectively.

To solve for m_1 and m_2 , we assume differentiated service with rate ν , where ν is a service differentiation parameter. Such a policy will assign service to both queues according to: $\mu_1 = \nu\mu_2$, and

$$\begin{aligned}15\pi_1(1 - \pi_2(1 - m_1)) &= 15\nu\pi_2(1 - \pi_1(1 - m_2)) \\ (1 - m_1) - \nu(1 - m_2) &= \frac{\pi_1 - \nu\pi_2}{\pi_1\pi_2}\end{aligned}\tag{C-3}$$

The second equation needed to solve for m_2 and m_1 is

$$m_1 + m_2 = 1\tag{C-4}$$

since we cannot assign more than 100% of the server capacity. Solving the two equations yields,

$$m_1 = \frac{1}{1 + \nu}\left(1 - \frac{\pi_1 - \nu\pi_2}{\pi_1\pi_2}\right)\tag{C-5}$$

and,

$$m_2 = \frac{1}{1 + \nu}\left(\nu + \frac{\pi_1 - \nu\pi_2}{\pi_1\pi_2}\right)\tag{C-6}$$

Substituting m_1 and m_2 in (C-1) and (C-2) above we get,

$$\mu_1 = \frac{15\nu}{1 + \nu}(\pi_1 + \pi_2 - \pi_1\pi_2)\tag{C-7}$$

and,

$$\mu_2 = \frac{15}{1 + \nu}(\pi_1 + \pi_2 - \pi_1\pi_2)\tag{C-8}$$

A special case is the fair scheduler, when $\nu = 1$, (i.e., $\mu_1 = \mu_2$). Then

$$m_1 = \frac{1}{2}\left(1 - \frac{\pi_1 - \pi_2}{\pi_1\pi_2}\right)$$

and,

$$m_2 = \frac{1}{2} \left(1 + \frac{\pi_1 - \pi_2}{\pi_1 \pi_2} \right)$$

Then (C-7) and (C-8) will be reduced to:

$$\mu_1 = \mu_2 = \frac{15}{2} (\pi_1 + \pi_2 - \pi_1 \pi_2) \quad (\text{C-9})$$

This formula can be used to estimate the service rate experienced by each user when applying a fair scheduling policy. Another interesting case, when $m_1 = m_2 = 1/2$. The service rates will be,

$$\mu_1 = 15\pi_1 \left(1 - \frac{\pi_2}{2} \right) \quad (\text{C-10})$$

and

$$\mu_2 = 15\pi_2 \left(1 - \frac{\pi_1}{2} \right) \quad (\text{C-11})$$

This case depicts the policy applied by Round Robin scheduler which divides the resources equally between the two users. From (C-10) and (C-11) we can see that the policy will result in a service differentiation that is highly dependent on the channel quality. The user with better channel quality will experience higher service rate than the other user. This policy is fair only if $\pi_1 = \pi_2$ and obviously unfair in every other situation.

References

- [1] 3GPP, *High Speed Downlink Packet Access (HSDPA): Overall Description (Release 5)*. 3GPP Technical specification, TS 25.308, V5.7.0, Dec 2004.
- [2] H. Wei, R. Izmailov, *Channel-Aware Soft Bandwidth Guarantee Scheduling for Wireless Packet Access*. IEEE Wireless Communications and Networking Conference (WCNC 04), March 2004.
- [3] H. R. Shao, C. Shen, D. Gu, J. Z and P. Orlik, *Dynamic Resource Control for High-Speed Downlink Packet Access Wireless Channel*. IEEE Transaction on Vehicular Technology, vol. 44, no. 1, Feb. 1995.
- [4] P. Bender, P. Black, M. Grob, R. Padovani, N. Sindhushayana, and A. Viterbi. *CDMA-HDR: A bandwidth-efficient high-speed wireless data service for nomadic users*. IEEE Communication Magazine, pages 7077, July 2000
- [5] T. Bonald, *A Score-Based Opportunistic Scheduler for Fading Radio Channels*. Proceeding of the European Wireless Conference, Barcelona, March 2004.
- [6] W. S. Jeon, D. G. Jeong, and B. Kim, *Packet Scheduler for Mobile Internet Services Using High Speed Downlink Packet Access*. IEEE Transactions on Wireless Communications, vol. 3, no. 5, Sept. 2004.
- [7] T. E. Kolding, F. Frederiksen and P. E. Mogensen, *Performance Aspects of WCDMA Systems with HSDPA*. IEEE 56th VTC, vol. 1, pp. 47781, 2002.
- [8] H. S. Wang and N. Moayeri, *Finite-State Markov Channel—A Useful Model for Radio Communication Channels*. IEEE Transactions on Vehicular Technology, vol. 44, pp. 163171, Feb. 1995.
- [9] M. Puterman, *Markov Decision Process: Discrete Stochastic Dynamic Programming*. USA: John wiley & Sons Inc., 1994.
- [10] H. Holma and A. Toskala, *WCDMA for UMTS, Radio Access for Third Generation Mobile Communication*, 3rd ed. USA: John wiley & Sons Inc., 2004.

- [11] J. P. Castro, *All IP in 3G CDMA Networks*. USA: John Wiley & Sons Inc., 2004.
- [12] S. M. Ross, *Introduction to Stochastic Dynamic Programming*. USA: Academic Press, 1983.
- [13] L. Tassiulas and A. Ephremides, *Dynamic server allocation to parallel queues with randomly varying connectivity*. IEEE Transactions on Information Theory, Vol. 39, Issue 2, Page(s):466 - 478, Mar. 1993.